



Subject A214

Actuarial Economic Modelling

(previously known as Financial Engineering and Loss Reserving)

Intermediate Technical Syllabus

For the 2025 Examinations

October 2024



Aim

The aim of the Actuarial Economic Modelling subject is to provide a grounding in the principles of modelling as applied to actuarial work – focusing particularly on stochastic asset and liability models, and the valuation of financial derivatives. These skills are also required to communicate with other financial professionals, and to critically evaluate modern financial theories.

Competencies

On successful completion of this subject, a student will be able to:

1. describe, interpret and discuss the theories on the behaviour of financial markets.
2. discuss the advantages and disadvantages of different measures of investment risk.
3. describe, construct, interpret and discuss the models' underlying asset valuations.
4. describe, construct, interpret and discuss the models' underlying liability valuations.
5. describe, construct, interpret and discuss the models' underlying option pricing.

Links to other subjects

Concepts introduced in A111 – Actuarial Statistics, A112 – Business Economics, A211 – Financial Mathematics, A212 – Risk Modelling and Survival Analysis and A213 – Contingencies are used in this subject.

Topics in this subject are further built upon in A311 – Actuarial Risk Management, N311 – Core Actuarial Professional Practice, F105 – Finance and Investment Principles and F106 – Enterprise Risk Management Principles.

Syllabus topics

1. Rational economic theory (10%)
2. Measures of investment risk (10%)
3. Asset valuations (30%)
4. Liability valuations (20%)
5. Option theory (30%)

The weightings are indicative of the approximate balance of the assessment of this subject between the main syllabus topics, averaged over a number of examination sessions.



The weightings also have a correspondence with the amount of learning material underlying each syllabus topic. However, this will also reflect aspects such as:

- the relative complexity of each topic, and hence the amount of explanation and support required for it.
- the need to provide thorough foundation understanding on which to build the other objectives.
- the extent of prior knowledge which is expected.
- the degree to which each topic area is more knowledge or application based.

Skill levels

The use of a specific command verb within a syllabus objective does not indicate that this is the only form of question which can be asked on the topic covered by that objective. The Examiners may ask a question on any syllabus topic using any of the agreed command verbs, as are defined in the document "Command verbs used in the Associate and Fellowship written examinations".

Questions may be set at any skill level: Knowledge (demonstration of a detailed knowledge and understanding of the topic), Application (demonstration of an ability to apply the principles underlying the topic within a given context) and Higher Order (demonstration of an ability to perform deeper analysis and assessment of situations, including forming judgements, taking into account different points of view, comparing and contrasting situations, suggesting possible solutions and actions, and making recommendations).

In the A214 subject, the approximate split of assessment across the three skill types is 5% Knowledge, 75% Application and 20% Higher Order skills.

Detailed Syllabus objectives

1. Rational economic theory (10%)

1.1 Rational expectations theory

- 1.1.1 Discuss the three forms of the Efficient Markets Hypothesis and their consequences for investment management.
- 1.1.2 Describe briefly the evidence for or against each form of the Efficient Markets Hypothesis.

1.2 Rational choice theory

- 1.2.1 Explain the meaning of the term "utility function".
- 1.2.2 Explain the axioms underlying utility theory and the expected utility theorem.
- 1.2.3 Explain how the following economic characteristics of investors can be expressed mathematically in a utility function:
 - non-satiation
 - risk aversion, risk neutrality and risk seeking



- declining or increasing absolute and relative risk aversion
- 1.2.4 Discuss the economic properties of commonly used utility functions.
- 1.2.5 Discuss how a utility function may depend on current wealth and discuss state dependent utility functions.
- 1.2.6 Perform calculations using commonly used utility functions to compare investment opportunities.
- 1.2.7 Analyse simple insurance problems in terms of utility theory.

2. Measures of investment risk (10%)

2.1 Properties of risk measures

- 2.1.1 Define the following measures of investment risk:
 - variance of return
 - downside semi-variance of return
 - shortfall probabilities
 - Value at Risk (VaR) / Tail VaR
- 2.1.2 Describe how the risk measures listed in 2.1.1 above are related to the form of an investor's utility function.
- 2.1.3 Perform calculations using the risk measures listed in 2.1.1 above to compare investment opportunities.
- 2.1.4 Explain how the distribution of returns and the thickness of tails will influence the assessment of risk.

2.2 Risk and insurance companies

- 2.2.1 Describe how insurance companies help to reduce or remove risk.
- 2.2.2 Explain what is meant by the terms "moral hazard" and "adverse selection".

3. Asset valuations (30%)

3.1 Mean-Variance portfolio theory

- 3.1.1 Describe and discuss the assumptions of mean-variance portfolio theory.
- 3.1.2 Discuss the conditions under which application of mean-variance portfolio theory leads to the selection of an optimum portfolio.
- 3.1.3 Calculate the expected return and risk of a portfolio of many risky assets, given the expected return, variance and covariance of returns of the individual assets, using mean-variance portfolio theory.
- 3.1.4 Explain the benefits of diversification using mean-variance portfolio theory.

3.2 Asset pricing models

- 3.2.1 Describe the assumptions, principal results and uses of the Sharpe-Lintner- Mossin Capital Asset Pricing Model (CAPM).
- 3.2.2 Discuss the limitations of the basic CAPM and some of the attempts that have been made to develop the theory to overcome these



limitations.

3.2.3 Perform calculations using the CAPM.

3.2.4 Discuss the main issues involved in estimating parameters for asset pricing models.

3.3 Single and multifactor models for investment returns

3.3.1 Describe the three types of multifactor models of asset returns:

- macroeconomic models
- fundamental factor models
- statistical factor models

3.3.2 Discuss the single index model of asset returns.

3.3.3 Discuss the concepts of diversifiable and non-diversifiable risk.

3.3.4 Discuss the construction of the different types of multifactor models.

3.3.5 Perform calculations using both single and multifactor models.

3.4 Stochastic models for security prices

3.4.1 Discuss the continuous time log-normal model of security prices and the empirical evidence for or against the model.

3.4.2 Explain the definition and basic properties of standard Brownian motion or Wiener process.

3.4.3 Demonstrate a basic understanding of stochastic differential equations, the Ito integral, diffusion and mean-reverting processes.

3.4.4 State Ito's Lemma and be able to apply it to simple problems.

3.4.5 Write down the stochastic differential equation for geometric Brownian motion and show how to find its solution.

3.4.6 Write down the stochastic differential equation for the Ornstein-Uhlenbeck process and show how to find its solution.

3.5 Models of the term structures of interest rates

3.5.1 Explain the principal concepts and terms underlying the theory of a term structure of interest rates.

3.5.2 Describe the desirable characteristics of models for the term-structure of interest rates.

3.5.3 Apply the term structure of interest rates to modelling various cash flows, including calculating the sensitivity of the value to changes in the term structure.

3.5.4 Describe, as a computational tool, the risk-neutral approach to the pricing of zero-coupon bonds and interest-rate derivatives for a general one-factor diffusion model for the risk-free rate of interest.

3.5.5 Demonstrate an awareness of the Vasicek, Cox-Ingersoll-Ross and Hull-White models for the term-structure of interest rates and their limitations

3.6 Simple models for credit risk

3.6.1 Define the terms credit event and recovery rate.

3.6.2 Describe the different approaches to modelling credit risk: structural models, reduced form models, intensity-based models.

3.6.3 Demonstrate a knowledge and understanding of the Merton



model.

- 3.6.4 Demonstrate a knowledge and understanding of a two-state model for credit ratings with a constant transition intensity.

4. Liability valuations (20%)

4.1 Ruin Theory

- 4.1.1 Explain what is meant by the aggregate claim process and the cash-flow process for a risk.
- 4.1.2 Use the Poisson process and the distribution of inter-event times to calculate probabilities of the number of events in a given time interval and waiting times.
- 4.1.3 Define a compound Poisson process and calculate probabilities using simulation.
- 4.1.4 Define the probability of ruin in infinite/finite and continuous/discrete time and state and explain relationships between the different probabilities of ruin.
- 4.1.5 Define the adjustment coefficient and explain and apply Lundburg's inequality.
- 4.1.6 Describe the effect on the probability of ruin, in both finite and infinite time, of changing parameter values by reasoning or simulation.
- 4.1.7 Describe and apply maximization of the adjustment coefficient under proportional reinsurance and excess of loss reinsurance.
- 4.1.8 Calculate probabilities of ruin by simulation.

4.2 Run-off Triangles

- 4.2.1 Define a development factor and show how a set of assumed development factors can be used to project the future development of a delay triangle.
- 4.2.2 Describe and apply a basic chain ladder method for completing the delay triangle using development factors.
- 4.2.3 Show how the basic chain ladder method can be adjusted to make explicit allowance for inflation.
- 4.2.4 Describe and apply the average cost per claim method for estimating outstanding claim amounts.
- 4.2.5 Describe and apply the Bornhuetter-Ferguson method for estimating outstanding claim amounts.
- 4.2.6 Describe how a statistical model can be used to underpin a run-off triangles approach.
- 4.2.7 Discuss the assumptions underlying the application of the methods in 4.2.1 to 4.2.6 above.

4.3 Value basic benefit guarantees using simulation techniques.

5. Option theory (30%)



5.1 Option Pricing and valuations

- 5.1.1 State what is meant by arbitrage and a complete market.
- 5.1.2 Outline the factors that affect option prices.
- 5.1.3 Derive specific results for options that are not model dependent:
 - show how to value a forward contract.
 - develop upper and lower bounds for European and American call and put options.
- 5.1.4 Explain what is meant by put-call parity.

5.2 Binomial option-pricing model and its application

- 5.2.1 Show how to use binomial trees and lattices in valuing options and solve simple examples.
- 5.2.2 Derive the risk-neutral pricing measure for a binomial lattice and describe the risk-neutral pricing approach to the pricing of equity options.
- 5.2.3 Explain the difference between the real-world measure and the risk-neutral measure. Explain why the risk-neutral pricing approach is seen as a computational tool (rather than a realistic representation of price dynamics in the real world).
- 5.2.4 State the alternative names for the risk-neutral and state-price deflator approaches to pricing.
- 5.2.5 Apply the state-price deflator approach to the binomial model and understand its equivalence to the risk-neutral pricing approach.

5.3 Black-Scholes derivative-pricing model

- 5.3.1 Demonstrate and utilize the martingale representation theorem.
- 5.3.2 Derive the Black-Scholes partial differential equation both in its basic and Garman-Kohlhagen forms.
- 5.3.3 Show how to use the Black-Scholes model to price and hedge a simple derivative contract using the martingale approach.
- 5.3.4 Show how to use the Black-Scholes model in valuing options and solve simple examples.
- 5.3.5 Describe and apply in Black-Scholes model, the approach to pricing using deflators and demonstrate its equivalence to the risk-neutral pricing approach.
- 5.3.6 Discuss the validity of the assumptions underlying the Black-Scholes model.
- 5.3.7 Demonstrate an awareness of the commonly used terminology for the first, and where appropriate second, partial derivatives (the Greeks) of an option price.

Assessment

Combination of a one-hour and forty-five-minute computer-based modelling assignment and a three-hour and fifteen-minute written examination.



End of Syllabus